

# Applied Geostatistics (G17604-01)

## - Final Examination -

**Student ID:**

**Name:**

### Notice

- Solve all problems by hand or using a computer program.
- Scan your solution as \*.pdf or \*.word file and upload it on Cyber Campus before 12:00 PM on June 20, 2018.
- Follow the format that gives a name to your report or report file:  
(final)-(student ID)-(last name)  
**For example, Seoyoon Kwon's filename must be final-181ERG01-Kwon.**
- **NO** discussion is allowed in this take-home examination.
- Fill your name in the following:  
*"I, \_\_\_\_\_, swear I solve all problems by myself in this final examination.  
I will take any disadvantages if any dishonesty such as cheating is acted on my solution."*

**Problem 1.**

Explain the following schemes briefly:

- (1) Second order stationarity [3 pts.]
- (2) Weak second order stationarity [3 pts.]
- (3) Intrinsic hypothesis [3 pts.]
- (4) Ergodicity [3 pts.]

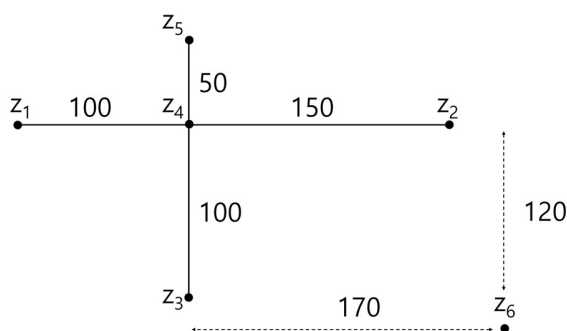
**Problem 2.**

Let's assume you have  $n$  sample data points.

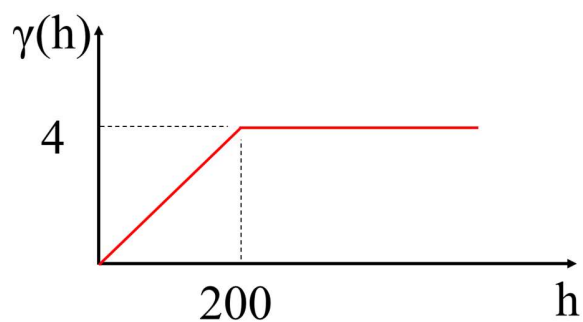
- (1) Derive the Kriging equation and the error variance for simple kriging [4 pts.].
- (2) Derive the Kriging equation and the error variance for ordinary kriging [4 pts.].
- (3) Derive the Kriging equation and the error variance for block kriging [4 pts.].
- (4) Derive the Kriging equation and the error variance for co-kriging [4 pts.].
- (5) Derive the Kriging equation and the error variance for co-block kriging [4 pts.].

**Problem 3. [20 pts.]**

You are given a variogram model, which is linear with the range of 200 and sill of 4 (i.e.,  $\gamma(h) = 4\text{Linear}_{200}(h)$ ). Estimate kriged values and its error variance values at  $z_4$ ,  $z_5$ , and  $z_6$  using simple kriging. Compare the estimates obtained using simple kriging with those obtained using ordinary kriging. Here, three sample values are as follows:  $z_1 = 5$ ,  $z_2 = 10$ , and  $z_3 = 15$ . Round any number off to the third decimal place for your calculation.



(a) Distribution of sample data  $z_1$ ,  $z_2$ , and  $z_3$



(b) Variogram model (linear)

**Problem 4.**

- (1) Explain the Exactness of Kriging briefly [5 pts].
- (2) Describe a procedure of cross validation in Kriging in brief [5 pts].
- (3) Perform Cross Validation for the **Problem 3** using ordinary kriging. Is the Exactness of Kriging is guaranteed in cross validation? [5 pts].

**Problem 5.**

- (1) Re-solve the Problem 3 using ordinary kriging with the following variogram model: [5 pts]

$$\gamma(h) = 4\text{Linear}_{400}(h)$$

- (2) Re-solve the Problem 3 using ordinary kriging with the following variogram model: [5 pts]

$$\gamma(h) = 8\text{Linear}_{200}(h)$$

- (3) Re-solve the Problem 3 using ordinary kriging with the following variogram model: [5 pts]

$$\gamma(h) = 4\text{Sph}_{200}(h)$$

- (4) Re-solve the Problem 3 using ordinary kriging with the following variogram model: [5 pts]

$$\gamma(h) = 4\text{Exp}_{200}(h)$$

- (5) Re-solve the Problem 3 using ordinary kriging with the following variogram model: [5 pts]

$$\gamma(h) = 4\text{Gauss}_{200}(h)$$

- (6) Describe effects of variogram parameters based on your Kriging results [4 pts].

- (7) Draw nugget, linear, exponential, and Gaussian variogram models with the range of  $a$  and sill of  $\sigma^2$  [4 pts].

----- This is the end of Final Examination for Applied Geostatistics. -----